

Multiplication and Division Progression Policy

Early Multiplication

- I can count in 2s, 5s and 10s



10



20



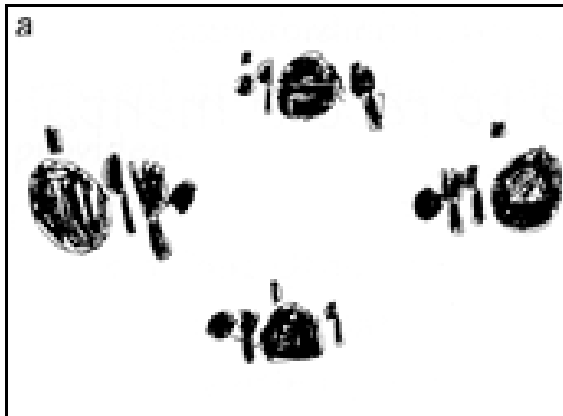
30



40

$$4 \times 10 = \underline{40}$$

- I can place objects in equal sized groups



$$4 \times 5 = \underline{20}$$

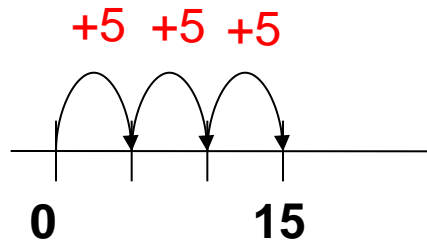
$$4 \text{ groups of } 5 = \underline{20}$$

Early Multiplication

- I can link multiplication to repeated addition



3 lots of 5 = $5 + 5 + 5$

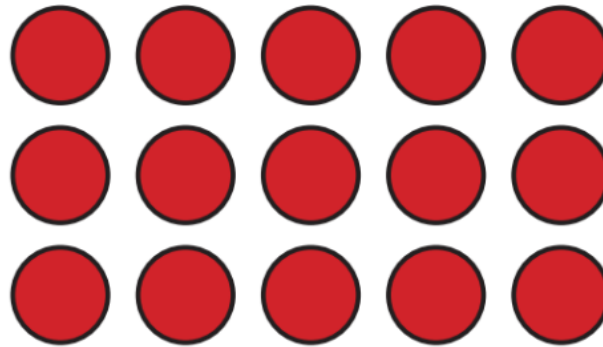


$3 \times 5 = \underline{15}$

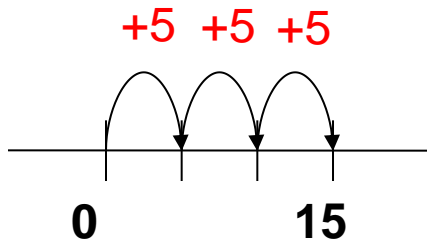
Use the counting on number line

Early Multiplication

- I can make arrays to show multiplication

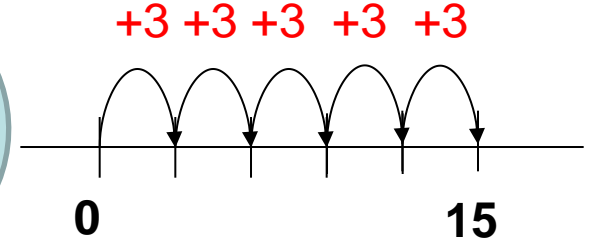


$$3 \times 5 = 5 + 5 + 5$$

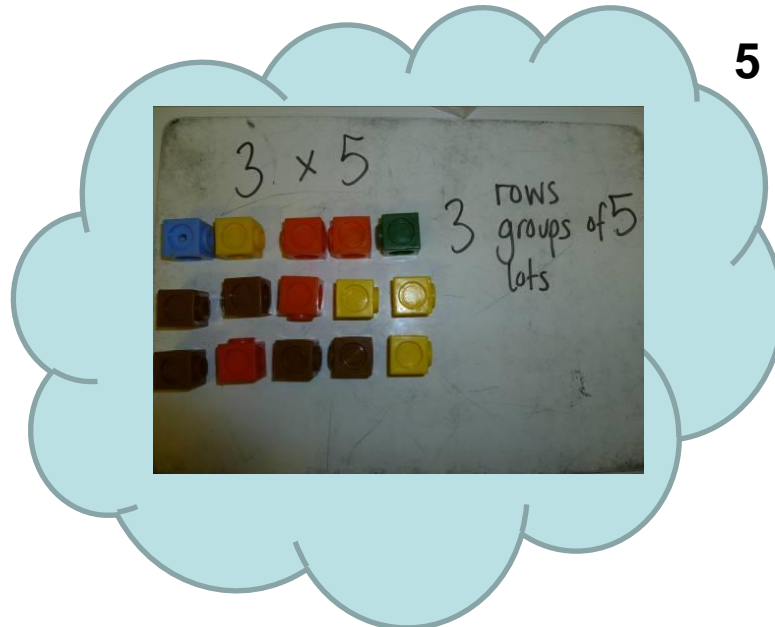


$$3 \times 5 = \underline{15}$$

$$5 \times 3 = 3 + 3 + 3 + 3 + 3$$



$$5 \times 3 = \underline{15}$$

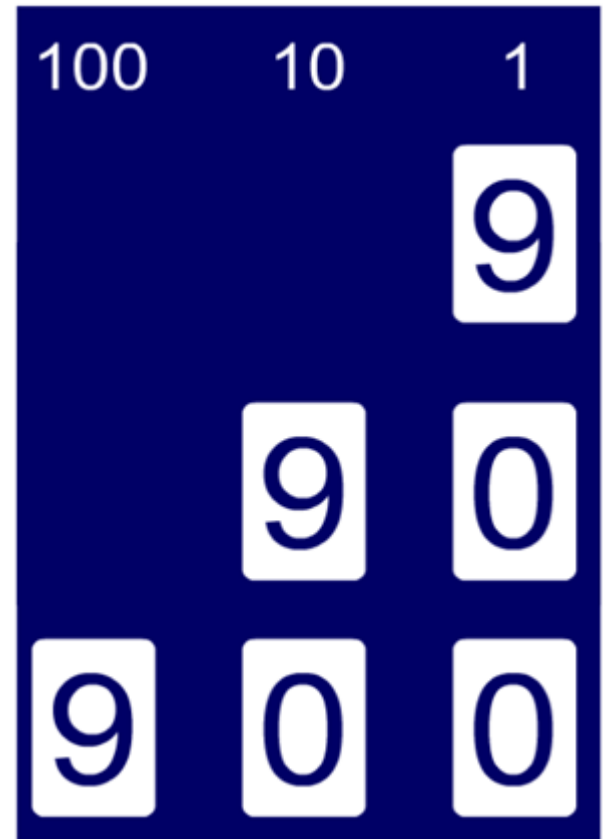


Multiplying by 10 and 100

- I can multiply numbers by 10 and 100 using a place value grid

$$9 \times 10 = \underline{90}$$

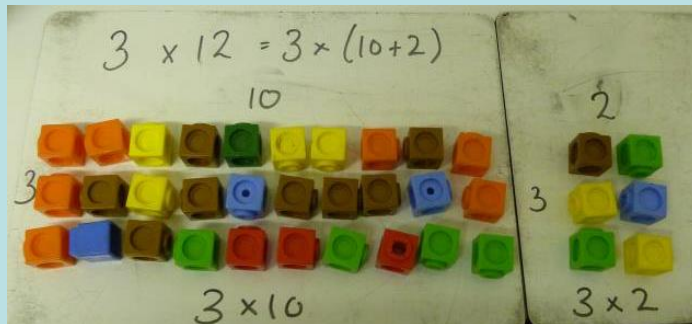
$$9 \times 100 = \underline{900}$$



Moving Forward

- I can partition numbers to simplify multiplication.

$$3 \times 12 = 3 \times 10 + 3 \times 2$$

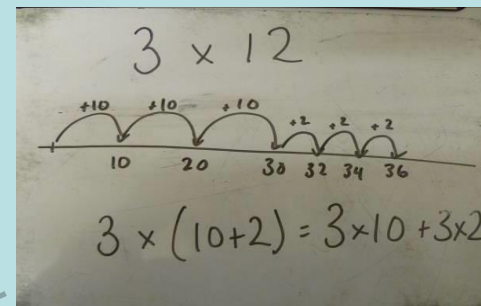


$$3 \times 10 = 30$$

$$3 \times 2 = 6$$

$$30 + 6 = \underline{36}$$

You can also show this on a number line



Moving Forward

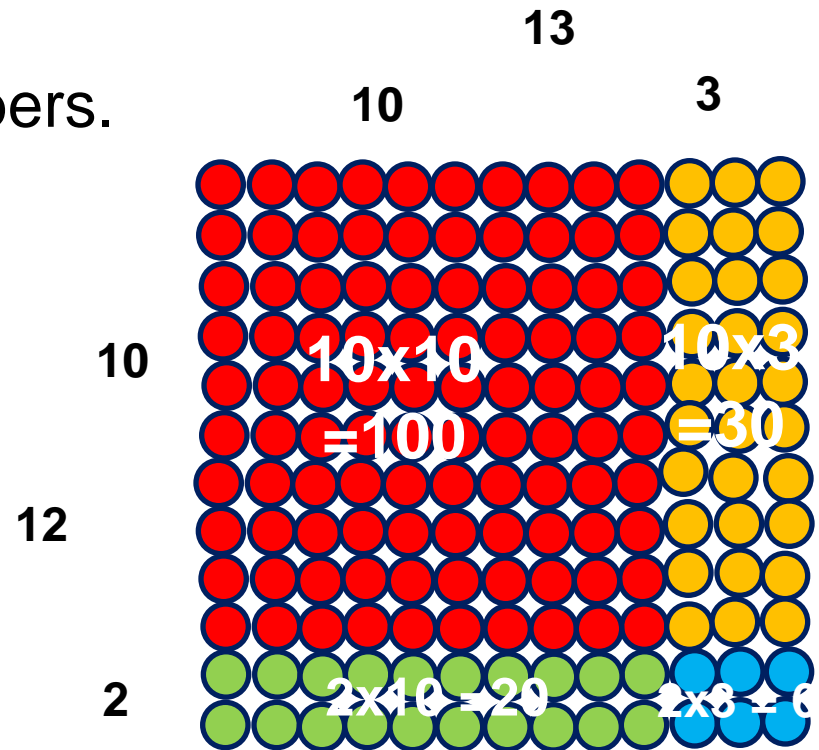
- I can use a written method for multiplication.

$$\begin{array}{r} 3 \times 12 = 3 \times 10 = 30 \\ + 3 \times 2 = 6 \\ \hline 30 + 6 = \underline{36} \end{array}$$

- I can multiply 2 digit numbers.

$$\begin{array}{r} 13 \times 12 = 13 \times 10 = 130 \\ + 13 \times 2 = 26 \\ \hline \end{array}$$

Your knowledge of times tables up to 10 x 10 and multiplying by 10 needs to be secure now!



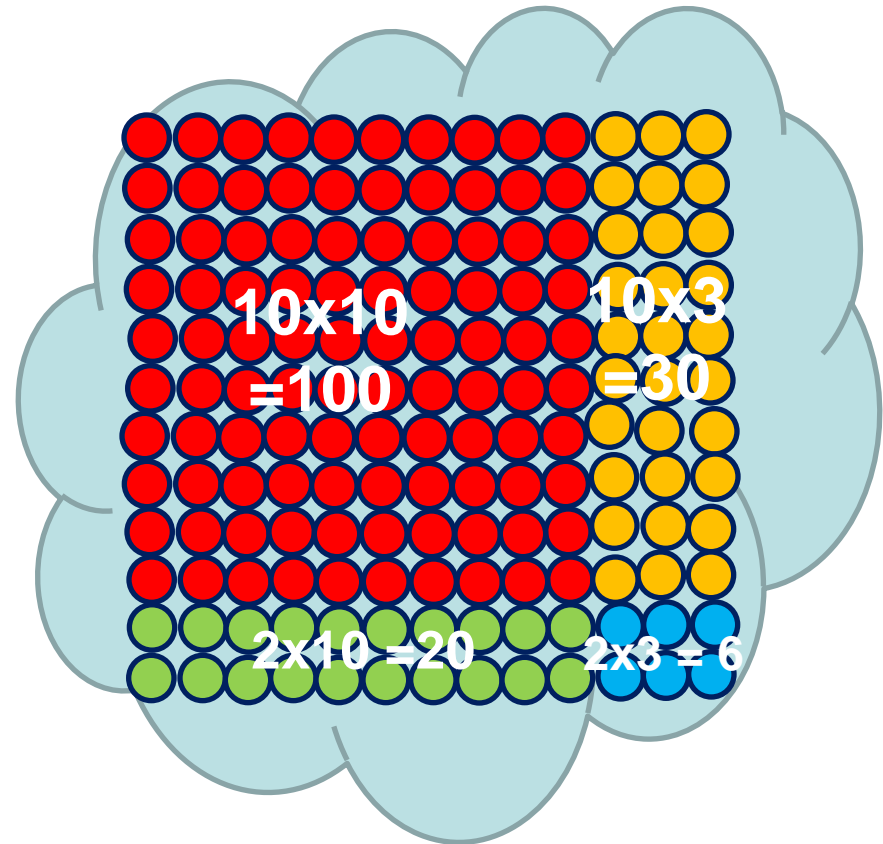
Moving Forward

- I can use a written method for multiplication.

13 x 12

x	10	2
10	100	20
3	30	6

$$120 + 36 = 156$$



$$13 \times 10 = 130$$

$$13 \times 2 = 26$$

Extending the Grid Method

- I can use the grid method to solve larger multiplication problems.

14 x 56

You must be secure with multiplying by multiples of 10
(e.g. $10 \times 5 = 50$, $10 \times 50 = 500$)

Estimate before carrying out
a calculation, so you
recognise if you make a
mistake.

x	50	6
10	500	60
4	200	24

Estimate!
 $10 \times 60 =$
600

500
200
60
+24
784

$500 + 200 + 60 + 24 = \underline{784}$

Multiplying Decimals

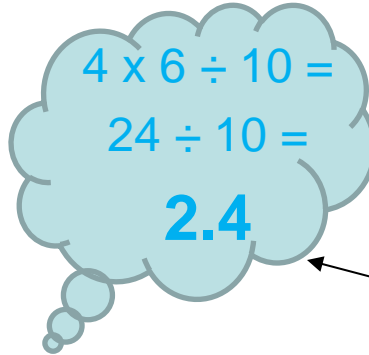
- I can use know facts to solve decimal multiplication

$$4 \times 3.6$$

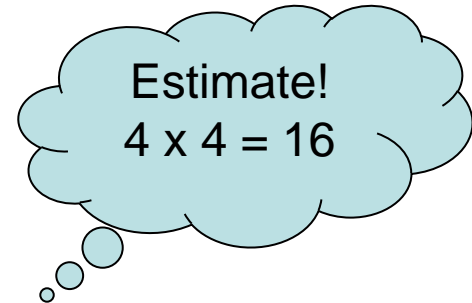
$$4 \times 3 = 12$$

$$4 \times 0.6 = 2.4$$

$$12 + 2.4 = 14.4$$



$4 \times 6 \div 10 =$
 $24 \div 10 =$
2.4



Estimate!
 $4 \times 4 = 16$

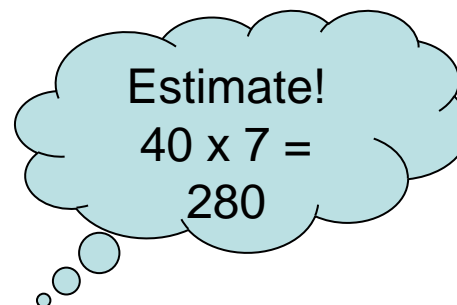
You must be secure at dividing by 10.

Moving Towards the Compact Multiplication Method

- I can use expanded multiplication

38 x 7

$$\begin{array}{r} 38 \\ \times 7 \\ \hline 56 \quad (8 \times 7) \\ + 210 \quad (30 \times 7) \\ \hline \underline{266} \end{array}$$



Compact Multiplication Method

$$24 \times 37$$

		24
X		37
<hr/>		
	168	
	720	
<hr/>		
	888	

$$(24 \times 7)$$

$$(24 \times 30)$$

Estimate!
 $20 \times 40 =$
800

Use what you know
to do this!
 $(7 \times 4) + (7 \times 20)$
 $24 \times 3 \times 10$

Using what you know...

To know my times tables, all I really need to know is 1 x and 10 x...

$$1 \times 6 = 6$$

$$2 \times 6 = 12 \text{ (double } 1 \times 6 \text{)}$$

$$3 \times 6 = 18 \text{ (} 1 \times 6 + 2 \times 6 \text{)}$$

$$4 \times 6 = 24 \text{ (double } 2 \times 6 \text{)}$$

$$5 \times 6 = 30 \text{ (half of } 10 \times 6 \text{)}$$

$$6 \times 6 = 36 \text{ (} 5 \times 6 + 1 \times 6 \text{ OR double } 3 \times 6 \text{)}$$

$$7 \times 6 = 42 \text{ (} 5 \times 6 + 2 \times 6 \text{)}$$

$$8 \times 6 = 48 \text{ (double } 4 \times 6 \text{)}$$

$$9 \times 6 = 54 \text{ (} 10 \times 6 - 1 \times 6 \text{)}$$

$$10 \times 6 = 60$$

$$1 \times 16 =$$

$$2 \times 16 =$$

$$3 \times 16 =$$

$$4 \times 16 =$$

$$5 \times 16 =$$

$$6 \times 16 =$$

$$7 \times 16 =$$

$$8 \times 16 =$$

$$9 \times 16 =$$

$$10 \times 16 =$$

If I know...

3 x 24 then I know 30 x 24

If I know...

2 x 24 then I know 4 x 24

$$34 \times 24 =$$

$$30 \times 24 + 4 \times 24$$

Early Division - Sharing

- I can share items into equal groups



12 items are shared into 3 equal groups
How many in each group?

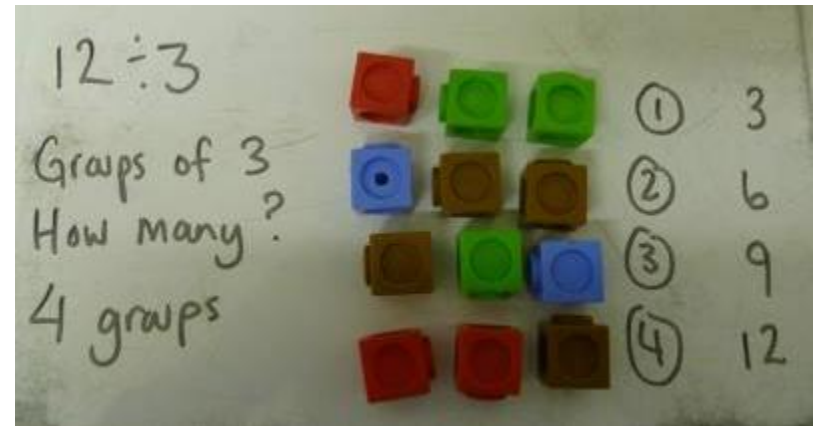
$$12 \div 3 = \underline{4}$$

12 shared into 3 groups is 4

÷ can mean
shared into groups of ...
or shared into ... groups

Early Division - Grouping

- I can group objects in a structured way



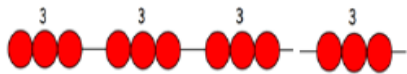
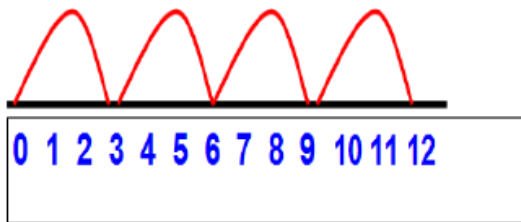
Can you spot the array?

It is really important you think about grouping in a structured way, instead of piles, as this will help with moving to written methods.

Division on the Number Line

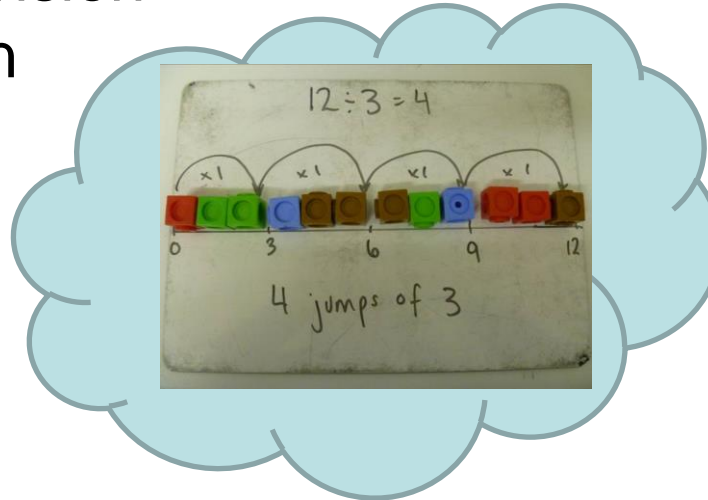
- I can understand division as repeated addition

$$12 \div 3 =$$



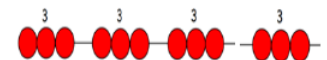
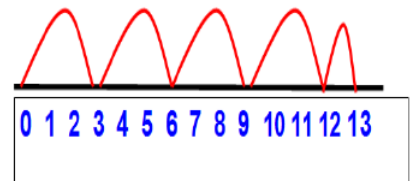
$$12 \div 3 = 4$$

Link to know facts:
 $3 \times 4 = 12$



*Move on to -
repeated addition
with remainders*

$$13 \div 3 =$$



$$12 \div 3 = 4 \text{ r } 1$$

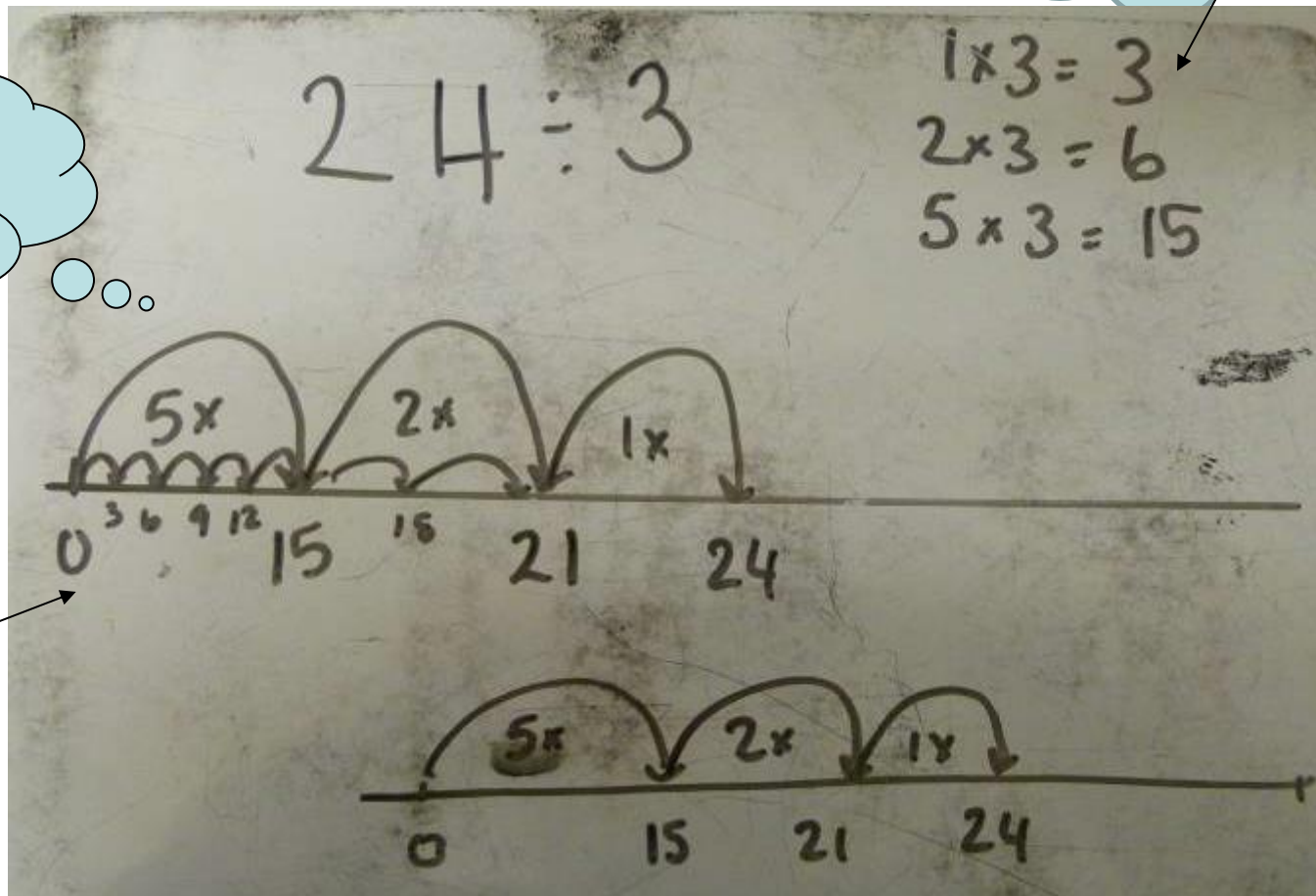
Becoming More Efficient...

- I can group the divisor to help divide larger numbers

Beginning to build a menu of known facts.

Estimate!
Less than 10,
because $3 \times 10 = 30$

Instead of single jumps of 3, I can use my times tables to help me since I know what 5 groups of 3 equals.



5 jumps + 2 jumps + 1 jump = 8 jumps

Division Using a Menu

You need to know your 1, 2, 5 times tables and also know how to build a menu of known facts to help become efficient at written division.

Single 1x
Double 2x
Medium 5x
Large 10x
X-Large 20x
Mega 50x
Super Size 100x

A 'Menu' can then be built for any number, helping to 'see' the larger jumps to be more efficient.

20 x 8 =
160, so less
than 20.

$$156 \div 8$$

$$\text{Single } 1x \ 8 = 8$$

$$\text{Double } 2x \ 8 = 16$$

$$\text{Medium } 5x \ 8 = 40$$

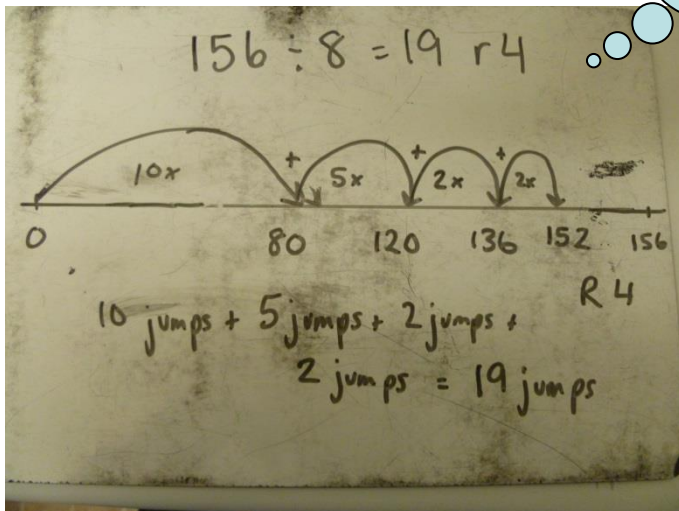
$$\text{Large } 10x \ 8 = 80$$

$$\text{X-Large } 20x \ 8 = 160$$

$$\text{Mega } 50x \ 8 = 400$$

$$\text{Super Size } 100x \ 8 = 800$$

Use of knowledge
of multiplying by 10

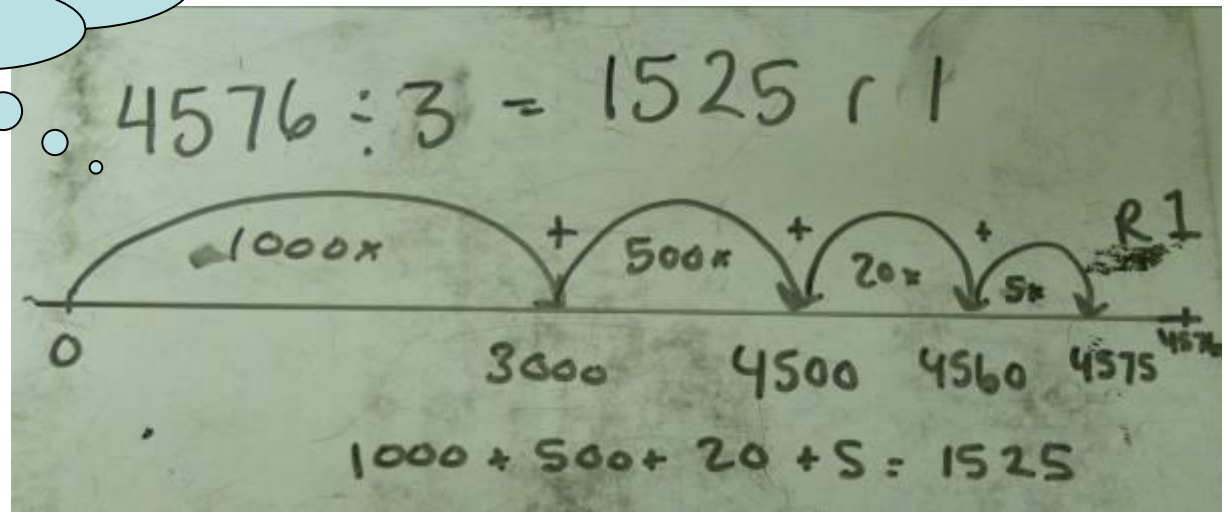


Using a Menu For Any Number

As you progress, you can build menus for any number, including decimals. You can adapt your menus as numbers get larger to include jumps of 200, 500, 1000 etc.

More than 1000, less than 2000 since $1000 \times 3 = 3000$ and $2000 \times 3 = 6000$.

- Single $1 \times 3 = 3$
- Double $2 \times 3 = 6$
- Medium $5 \times 3 = 15$
- Large $10 \times 3 = 30$
- X-Large $20 \times 3 = 60$
- Mega $50 \times 3 = 150$
- Super Size $100 \times 3 = 300$
- Gigantic $200 \times 3 = 600$
- Enormous $500 \times 3 = 1500$
- Huge $1000 \times 3 = 3000$



Moving Towards Compact Methods

- I can divide a number by subtracting multiples of the divisor

$$965 \div 5$$

$$100 \times 5 = 500$$

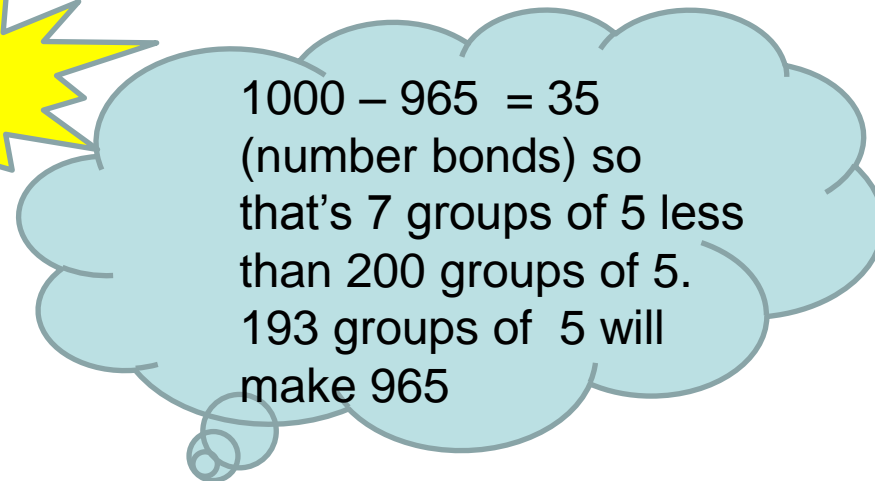
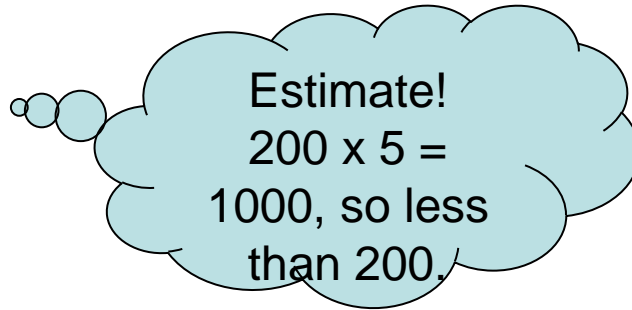
465 left..

$$90 \times 5 = 450$$

15 left...

$$3 \times 5 = 15$$

$$965 \div 5 = 193$$



$$\begin{array}{r} 193 \\ 5 \overline{) 965} \\ \underline{- 500} \\ 465 \\ \underline{- 450} \\ 15 \end{array}$$

A Semi-Compact Method

- I can use a semi-compact division method

$$357 \div 6 =$$

		5	9		R 3	
6)	3	5	7		
		3	0			
			5	7		
				3		

$$357 \div 6 = 59 \text{ r } 3$$

The Compact Method

- I can use a compact division method

$$357 \div 6 =$$

		5	9	r3		
6)	3	5	7		

□

$$357 \div 6 = 59 \text{ r}3$$

The Compact Method including Remainder as a Decimal

- I can use a compact division method

$$3859 \div 6 =$$

		6	4	3	.	1	7	
6)	3	³ 8	² 5	¹ 9	.	¹ 0	⁴ 0

$$3859 \div 6 = 643.17$$

(to 2 dp)